

## Dissecting Between-Plant and Within-Plant Wage Dispersion - Evidence From Germany

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## Dissecting between-plant and within-plant wage dispersion – Evidence from Germany\*

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#### Abstract

Using rich linked employer-employee data for (West) Germany between 1996 and 2014, we analyze the most important drivers of the recent rise in German wage dispersion and pin down the relative contribution of plant and worker characteristics. Moreover, we separately investigate the drivers of between-plant and within-plant wage dispersion. We also analyze the sources of the recent slowdown in German wage inequality and compare the results for West Germany to the ones for East Germany. We disentangle the relative contribution of each single variable to the rise in wage dispersion using recentered influence function (RIF) regressions. The most important drivers of wage dispersion are industry effects and the bargaining regime. The former predominantly works through the wage structure effect while, in the latter case, both the decline in collective bargaining coverage and the strong increase in wage dispersion within the group of covered plants have played a substantial role. While education has been another factor contributing to both between-plant and within-plant wage inequality, other candidate factors such as plant size, the exporting status, plant technology, and investment intensity are all of little if any direct quantitative importance for the increase in wage dispersion.

**Keywords:** Wage inequality; Decomposition; RIF-Regression; Linked employer-employee data

JEL classification: J 31; J51; C21; F16

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#### 1 Introduction

Wage inequality has been on the rise in most (industrialized) countries in the last few decades, and recent research has pointed to the growing importance of workplace heterogeneity for this development: a large fraction of the increase in overall wage inequality is due to increased wage dispersion between as opposed to within firms or plants. While this trend is shared by many countries, the drivers of this increase are still underexplored.<sup>1</sup>

Against this background, the aim of this paper is to pin down the role of central plant and worker characteristics for the increase in wage inequality, focusing on (West) Germany. For this purpose, we use detailed linked-employer-employee data, covering the years 1996 to 2014. We adopt a particularly rich framework and jointly evaluate the contributions of standard worker characteristics (age, education, occupation, and nationality) and an extensive set of plant characteristics (plant size, export status, collective bargaining coverage, existence of a works council, technological status, investment intensity, industry, and region). As a further central contribution, we separately analyze the sources of changes in between-plant and within-plant wage dispersion, thus shedding light on the (possibly divergent) drivers of these two important subcomponents of wage inequality and informing theoretical analyses.<sup>2</sup> In doing so, we also provide updated evidence on differences in the sources of upper-tail and lower-tail (between-plant) wage dispersion, respectively. Finally, we analyze the sources of the recent slowdown in German wage inequality (cf. Möller, 2016) and compare the results for West Germany to the ones for East Germany.

Disentangling the role of each single variable to the rise in wage dispersion, taking other variables explicitly into account, is politically relevant. An increase in overall inequality due to demographic aging is valued differently as a similar increase driven by a higher wage gap between skill groups. However, quantifying the relative contributions of various factors to rising inequality in a unified framework, both through compositional changes and changes in the conditional wage structure, is an empirical challenge. To this end, we apply a state-of-the-art decomposition method based on recentered influence function (RIF) regressions (Firpo et al., 2009). Crucially, compared to sequential decompositions, this approach has the further advantage of being path-independent.

Our main findings are as follows. First, we confirm that wage dispersion among fulltime male workers in Germany has risen strongly and fairly continuously between 1996 and 2010, but slightly declined thereafter. Both the strong increase and the subsequent slight decrease were driven by the between-plant as opposed to the within-plant component of wage dispersion.

Second, conditional on our extensive set of control variables, two employer-level characteristics are the most important drivers of wage dispersion: industry effects and the col-

<sup>&</sup>lt;sup>1</sup>Davis and Haltiwanger (1991), Dunne et al. (2004), and more recently, Barth et al. (2016), Handwerker and Spletzer (2016), and Song et al. (2015) provide evidence for the US; Faggio et al. (2010) for the UK; Card et al. (2013) for Germany; and Helpman et al. (2017) for Brazil. In contrast, the between-firm component seems to be less important in Sweden (Akerman et al., 2013).

<sup>&</sup>lt;sup>2</sup>Note that even a (hypothetically) important contribution of plant-level characteristics to overall wage inequality does not necessarily imply that these factors are also the drivers of increased between-plant wage dispersion. Instead, they could also be associated with higher within-plant wage inequality. By the same token, individual-level characteristics (and the returns to them) could well be responsible for increased between-plant wage dispersion, e.g. through increased sorting.

lective bargaining regime. The former matters in terms of the wage structure effect while, in the case of collective bargaining, both the composition and the wage structure play a substantial role. The former reflects the strong decline in collective bargaining coverage and the latter is due to both an increase in the wage gap between covered and uncovered plants and a strong increase in wage dispersion within the group of covered plants. According to the point estimates of the decomposition results, the effects associated with the industry and the collective bargaining regime together account for more than 100 percent of the total increase in the log wage variance between 1996 and 2010, where one has to take into account that several other factors are associated with declining wage dispersion. Both the industry and collective bargaining have affected wage dispersion in very specific ways. They are sources of increasing between-plant wage dispersion, but they are, if at all, negatively related to within-plant wage inequality. Moreover, they have affected lower-tail as opposed to upper-tail (between-plant) wage inequality.

Third, in terms of individual-level characteristics, education is the one that matters the most where both employment shifts towards more highly skilled workers and, even more so, changes in the skill-related wage structure, particularly in the wage gap between high-educated and low-educated workers, have played important roles. They contributed to both within-plant and between-plant wage dispersion. Interestingly, we find that the skill-related wage structure effect, in particular, is quantitatively even more important for between-plant than for within-plant wage inequality, reflecting that a major part of changes in the skill-wage gaps has arisen from increasing between-establishment wage differentials. We attribute this finding to increased assortative matching along the skill dimension.

Fourth, just as interesting as the factors that have contributed the most to rising wage dispersion are the ones that have not. Plant size, the exporting status, plant technology, and investment per worker are all of little if any quantitative importance for the increase in wage dispersion. This is remarkable given that many potential culprits for the increase in wage inequality such as the rise of superstar firms, globalization, and technological change could be expected to materialize (at least partly) via these channels. It also underscores that simple, monocausal explanations for the rise in wage dispersion do not exist and that the impact of drivers such as international trade may be having indirect (e.g., by affecting institutions) rather than direct effects.

This paper builds on and contributes to a rich existing literature on wage inequality, where the German experience has recently attracted a lot of interest. Indeed, Germany is an interesting case in point, as it has long been known for a rather stable wage distribution, but in the last few decades experienced a strong increase in wage inequality. In fact, the German wage structure shares many of the developments observed in the US, although inequality at the bottom of the wage distribution started to rise only in the 1990s, one decade later than in the US (Dustmann et al., 2009). Previous research has already hinted at some important sources of rising (West) German wage inequality. In their seminal contribution, Dustmann et al. (2009) stress the importance of changes in workforce composition (in line with Lemieux, 2006) and the decline in collective bargaining.<sup>3</sup> In addition, they provide

<sup>&</sup>lt;sup>3</sup>In subsequent research, Dustmann et al. 2014 also point to greater wage flexibility within the covered sector, which they attribute to an increased use of "opening clauses" in industry-level collective agreements.

indicative evidence that technological change has played a role for the widening of the wage distribution at the top. In line with most earlier studies, Dustmann et al. (2009) mostly rely on plain individual-level data, the bargaining status of the plant being the only establishment-level characteristic considered.

Building upon these results, Antonczyk et al. (2010) use a sequential decomposition analysis based on quantile regressions in order to investigate the increase in wage inequality between 2001 and 2006. Using linked employer-employee data, they explicitly account for a number of personal as well as firm characteristics. According to their analysis, changes in collective bargaining play a significant, however minor role for the development of wage inequality once other firm-level variables are controlled for. They find that the largest contribution comes from wage differences within and between industries. While their paper is, in some aspects, similar in spirit to our analysis, we expand on it in important respects. First, we explicitly distinguish sources of between-plant and within-plant wage dispersion. Second, we account for several additional plant-level characteristics such as exporting, technology, and investment. Third, we consider a longer and more recent time period. Fourth, in terms of the methodology, our approach has the advantage of not depending on the sequential ordering of the decomposition.

More recent research puts special emphasis on the firm or establishment component of wage dispersion. Most notably, Card et al. (2013) use (West) German linked employeremployee data and document that about 60 percent of the increase in cross-sectional wage dispersion are due to establishment effects and the covariance between establishment and person effects. The exploration of the underlying sources of this growing importance of establishment-level pay is still in its infancy, however. Also, it is unclear to what extent increased between-establishment wage dispersion is linked to the drivers of aggregate wage inequality highlighted in the previous literature. Card et al. (2013) provide tentative evidence that the decline in collective bargaining discussed above has likely contributed to this development, yet they do not explore the quantitative importance of this channel.<sup>4</sup> Other research has focused on selected alternative (potential) drivers.<sup>5</sup> Goldschmidt and Schmieder (2017) analyze the importance of domestic (on-site) outsourcing of food, cleaning, security and logistics services and find that this channel can account for around 9 percent of the increase in German wage inequality since the 1980s. Turning to international evidence, Handwerker and Spletzer (2016), having in mind a similar hypothesis as Goldschmidt and Schmieder (2017), analyze whether an increasing concentration of occupations at establishments has played a role. They find that this channel can only account for a small amount of the increase in (between-establishment) wage dispersion in the US. Song et al. (2015), on the other hand, provide evidence that the increase in between-firm inequality in the US has been driven by increased employee segregation in terms of the worker-fixed pay component, where high- and low-paid employees are increasingly clustering in different firms. Other firm or establishment characteristics that have been found to be relevant – either for

<sup>&</sup>lt;sup>4</sup>Hirsch and Müller (2018) provide further evidence in this respect. They show that, in the cross section, establishment wage premia are indeed larger on average but less dispersed among plants covered by a collective agreement than among uncovered ones. Yet they do not explicitly analyze the role of the decline in collective bargaining for changes in (between-plant) wage dispersion over time.

<sup>&</sup>lt;sup>5</sup>See Card et al. (2018) for a summary of a rich literature on the determinants of firm-level pay, without however focusing on drivers of changes in these premia over time.

changes in overall wage inequality or for changes in between-establishment heterogeneity – are the industry of the workplace (Antonczyk et al., 2010; Barth et al., 2016) and the export status of the plant (Helpman et al., 2017; Baumgarten, 2013; Egger et al., 2013).<sup>6</sup>

Compared to these studies, we adopt a more agnostic, but also more comprehensive approach. Instead of pursuing one specific hypothesis, we account for a whole set of potential driving factors and quantify their respective contributions to the increase in overall as well as in between-plant and within-plant wage dispersion. While our decomposition analysis does not enable us to identify causal effects in a deeper, structural sense, we are able to identify the proximate sources of increased wage dispersion that any meaningful structural explanation should be consistent with.

The remainder of the paper is organized as follows. In Section 2, we describe the linked employer-employee data used for our analysis. In Section 3, we briefly discuss the key developments in the German wage structure. Section 4 explains the decomposition analysis. We present a first descriptive overview of changes in the composition of workers and plants as well as changes in the wage structure associated with worker and plant characteristics, the ingredients to our decomposition analysis, in Section 5. In Section 6, we provide a detailed discussion of our decomposition results. Section 7 concludes.

## 2 Data and sample restrictions

We base our analysis on the German LIAB data, which is a linked employer-employee data set provided by the Institute for Employment Research (IAB) in Nuremberg.<sup>8</sup> It combines the IAB Establishment Panel with social security data on all workers who were employed in one of the establishments as of the 30th of June of a given year.

The IAB Establishment Panel is a stratified sample of all establishments that employ at least one worker subject to social security. The strata variables are defined over regions, industries, and size classes. Appropriate weights, which are inverse to the sampling probability, are provided to assure the representativeness of the results. The IAB Establishment Panel started in 1993 with West-German plants, while East-German plants have been included from 1996 onwards. Although participation in the IAB Establishment Panel is voluntary, the response rate is very high (up to 80 percent for repeatedly interviewed

<sup>&</sup>lt;sup>6</sup>The focus on the export status is motivated by recent trade theories, which analyze the link between international trade and wage inequality in a setting with heterogeneous firms and labor market imperfections (e.g. Helpman et al., 2010; Egger and Kreickemeier, 2012; Felbermayr et al., 2018). In these models, the exporter wage premium, the wage differential between workers employed at exporters and the ones employed at non-exporters, is the key transmission channel from trade to wage inequality.

<sup>&</sup>lt;sup>7</sup>In work subsequent to ours, Biewen and Seckler (2017) have conducted a similar analysis, relying on an alternative data set, the German Structure of Earnings Surveys (GSES). These linked employer-employee data are provided by the German Federal Statistical Office. Biewen and Seckler (2017) also conduct a decomposition analysis based on RIF regressions to disentangle various sources of changes in German wage dispersion between 1995 and 2010. The downside of their data set is that it contains less firm-level variables. Moreover, the authors do not explicitly distinguish sources of between-plant and within-plant wage dispersion, and they do not consider the years after 2010, when German wage inequality was falling.

<sup>&</sup>lt;sup>8</sup>More precisely, this study uses the Linked-Employer-Employee Data (LIAB) [cross-sectional model 2 1993–2014 (LIAB QM2 9314)] from the IAB. Data access was provided via on-site use at the Research Data Centre (FDZ) of the German Federal Employment Agency (BA) at the Institute for Employment Research (IAB) and subsequently remote data access. See Klosterhuber et al. (2016) for a detailed description of the data.

establishments). The survey is very detailed and covers many different topics. Further plant-level variables such as the industry affiliation at the three-digit level and the region where the plant is located are provided from the Establishment History Panel.

The employee data are based on social security notifications made by the employer on behalf of their employees that are mandated by law. Hence, only workers covered by social security are included in these Employment Statistics, while civil servants and the self-employed are not. The data still cover, however, about 80 percent of the German workforce. These compulsory social security records contain personal information such as gender, the year of birth, citizenship, the level of education, the occupation (at a three-digit level), and the top-coded daily wage. Specifically, wages are right-censored at the contribution ceiling to the social security system. In our sample, between 9 and 14 percent of the wage observations are censored in every year. To address this problem, we follow Dustmann et al. (2009) and impute the missing upper tail of the wage distribution using a series of Tobit regressions.<sup>9</sup> Using the estimated parameters from these models, we replace each censored wage value with a random draw from the upper tail of the appropriate conditional wage distribution. All wage information is then converted into constant year-2000 euros by deflating them with the Consumer Price Index as provided by the German Federal Statistical Office.

Similar to previous research (e.g. Dustmann et al., 2009; Card et al., 2013), we limit our attention to full-time jobs held by men in the age range 18-65. We exclude marginal jobs that are subject to reduced social security contributions as well as workers that undergo training. For workers who hold multiple jobs, we only keep the highest-paying one. We exclude observations that are reported to have an (implausibly) low daily wage of less than ten euros. To be comparable to the earlier research cited above, and since West and East Germany are still characterized by substantially different labor markets and wage schedules, we focus on West Germany for the main part of our analysis. 10 Our period of analysis covers the years from 1996 to 2014. However, for the most part, we focus on the period 1996 to 2010, which was characterized by a fairly steady rise in wage dispersion (as we show in the next section below). In an extension, we also look at the more recent period from 2010 to 2014. Not only was this second (shorter) period characterized by a decline in wage dispersion, but also by some changes to the variables in the data set, which makes the separation of these two time periods – in our view – a reasonable choice. Taking these restrictions into account, we end up with 964,587 (614,483) workers and 3,433 (6,571) plants in 1996 (2010). It is worth noting that our sample restrictions, in particular due to the focus on full-time workers, may lead to an underestimation of the overall level and growth of wage inequality among German male workers. However, as the data do not contain information on the hours worked, including part-time workers would add too much noise to the analysis.

<sup>&</sup>lt;sup>9</sup>We run a series of Tobit regressions for each year, education group, and region (east/west). The explanatory variables are the ones that we also use in our decomposition analysis described below.

<sup>&</sup>lt;sup>10</sup>Moreover, we do not consider those establishments, where the reporting unit in the Establishment Panel has changed over time. This is due to the fact that such a change in the reporting unit might not be accompanied by a corresponding change in the workforce data since the latter's establishment id stays the same.

### 3 Trends in German wage inequality

Panel (a) of Figure 1 displays the evolution of overall wage inequality for our sample as measured by the variance of log real wages. It can be seen that wage dispersion has been rising fairly steadily (except for a dip in 2002) up to 2010 before declining slightly in the following three years and mildly rebouncing in 2014. In terms of magnitude, the increase between 1996 and 2010 (2014) amounts to about 77 percent (65 percent) of the initial value, which is substantial.

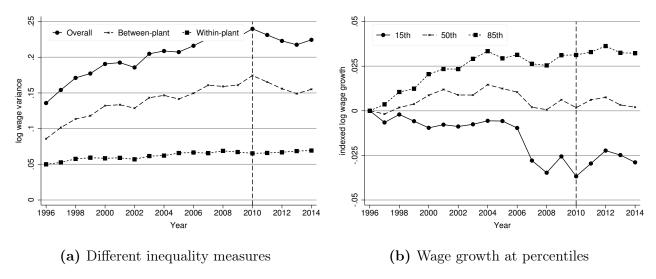


Figure 1. Evolution of wage dispersion

Notes: Figure (a) shows the evolution of overall, between-plant, and within-plant wage variance. We construct the measure of between-plant (within-plant) variance by using yearly regressions of log real individual wages on a full set of plant fixed effects. We then take the variance of predicted (residual) wages as a measure of between-plant (within-plant) inequality. Figure (b) shows indexed log real wage growth at the 15th, 50th, and 85th percentiles. Since at most 14 percent of wage observations are censored in each year, the 85th wage percentile is not affected. Both figures are based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany.

The figure also shows the development of between-plant and within-plant wage dispersion. The variance has the attractive property that the between and the within component add up to the total, fulfilling the criterion of an additively separable inequality measure (Shorrocks, 1980). Technically, this can be formalized as follows:

$$\underbrace{\frac{1}{N_{t}}\sum_{i}\left(w_{it}-\bar{w}_{t}\right)^{2}}_{\text{overall variance}} = \underbrace{\frac{1}{N_{t}}\sum_{j}N_{jt}\left(\bar{w}_{jt}-\bar{w}_{t}\right)^{2}}_{\text{between-plant variance}} + \underbrace{\frac{1}{N_{t}}\sum_{j}\sum_{i\in j}\left(w_{it}-\bar{w}_{jt}\right)^{2}}_{\text{within-plant variance}},$$

where workers are indexed by i and plants by j.  $N_t$  and  $N_{jt}$  denote the overall number of workers and the number or workers in plant j at time t, respectively. In addition,  $w_{it}$  denotes the log wage of individual i,  $\bar{w}_{jt}$  the mean log wage within plant j, and  $\bar{w}_t$  the overall mean log wage at time t.

While in 1996, the between-plant component already accounted for 63 percent of overall wage inequality, this share rose to 73 percent by 2010. Thus, this component contributed 85 percent to the increase in wage inequality over the main period of analysis. This is in

line with findings of the related literature, which also stresses the growing importance of between-plant wage dispersion. Interestingly, it is also the between-plant component which accounts for the decline in wage dispersion after 2010, while within-plant wage dispersion continued to increase, albeit modestly.

While the variance is a good and frequently used summary measure of overall wage dispersion, it does not allow one to analyze changes at different parts of the wage distribution. Therefore, Panel (b) of Figure 1 shows changes in log real wages over time at different percentiles of the earnings distribution (normalized to the year 1996). Workers at the median and at the 85th percentile have realized real wage gains, while workers at the 15th percentile have faced declines in real wages. The latter were particularly pronounced in the period 2006 to 2010, while they recovered slightly thereafter. Considering the 85-50 and 50-15 log wage differentials as measures of upper-tail and lower-tail wage inequality, respectively, it becomes apparent that the larger part of the overall increase in wage inequality between 1996 and 2010 was due to changes in the lower part of the earnings distribution.

## 4 Empirical approach and methodology

In order to quantify the relative importance of (changes in) various covariates for (changes in) the distribution of wages, our empirical approach has to meet different requirements: Firstly, it needs to allow us to "go beyond the mean", meaning that we need to estimate the effects not only at the mean but on the whole distribution of our dependent variable of interest. Secondly, we need to account for several covariates jointly in a comprehensive framework. This is because we are interested in the *conditional effects* of our covariates and on the impact of each covariate relative to the other included factors. Thirdly, for each single covariate, we would like to distinguish a composition effect, which is linked to changes in the distribution of this factor, and a wage structure effect that reflects changes in the conditional wage distribution over time. The latter two requirements are usually referred to as allowing for a *detailed decomposition*.

A decomposition method which can be applied beyond the mean and allows for a detailed decomposition with respect to each single covariate in a unified framework is the so called RIF regression approach, which is based on recentered influence function (RIF) regressions and was introduced by Firpo et al. (2009). A simple intuition for this methodology is that it can be regarded as a generalization of a standard Oaxaca-Blinder decomposition technique (Oaxaca, 1973; Blinder, 1973) from the mean to other distributional statistics. Apart from being computationally relatively simple, a key advantage of the RIF regression approach is that the decomposition results are path-independent. The latter property implies that we do not have to take a stand on the sequential ordering of covariates in the decomposition process, which generally matters in our decomposition methods.<sup>12</sup> In the following, we sketch the key technical details underlying our approach.<sup>13</sup>

<sup>&</sup>lt;sup>11</sup>Note that the subset of workers (and their characteristics) at each percentile might have changed over time. <sup>12</sup>Alternative approaches that also allow for detailed decompositions generally do not share the property of path independence, often face non-monotonicity problems, and are computationally more cumbersome (see e.g. Chernozhukov et al., 2013, DiNardo et al., 1996, Melly, 2005).

<sup>&</sup>lt;sup>13</sup>This section is very much based on Firpo et al. (2013) and Fortin et al. (2011). We refer the interested reader

A RIF regression is similar to a standard regression with the exception that the dependent variable Y is replaced by the recentered influence function of the statistic of interest. Consider IF(y;v), the influence function corresponding to an observed wage y for the distributional statistic  $v(F_Y)$  of interest (e.g., a quantile, the variance, the Gini coefficient). The recentered influence function is defined as  $RIF(y;v) = v(F_Y) + IF(y;v)$  so that it aggregates back to the statistic of interest:  $\int RIF(y;v) \cdot dF(y) = v(F_Y)$ . In non-technical terms, the influence function represents the contribution of a given observation to the distributional statistic of interest.

Assuming that the conditional expectation of RIF(y; v) can be modeled as a linear function of the explanatory variables,

$$E[RIF(y; v)|X] = X\gamma + \epsilon,$$

the corresponding parameters  $\gamma$  can be estimated by OLS. Applying this approach to quantiles, the RIF regression corresponds to an unconditional quantile regression, which allows one to estimate the marginal effect of any explanatory variable, say, the share of workers covered by collective bargaining, on the  $\tau$ th quantile of the wage distribution. Different from a standard conditional quantile regression, which only captures within-group (or residual) wage effects of the covariates, the unconditional quantile regression captures both withingroup and between-group effects. For example, in the case of collective bargaining, the (typically negative) within-group effect on wage inequality stems from the fact that within the covered sector, wages (among comparable workers) tend to be more compressed than in the non-covered sector. On the other hand, the (typically positive) between-group effects result from covered workers usually earning a higher conditional mean wage than non-covered workers. As this example illustrates, the within-group and the between-group effects may go into different directions, and one or the other may dominate at different points of the wage distribution. The RIF coefficients as such, however, do not allow disentangling the within-group and the between-group component so that we will resort to auxiliary evidence in cases where this distinction is of interest.

Due to the linearization, it is straightforward to apply the standard Blinder-Oaxaca decomposition to the RIF regression. Thus, if one is interested in decomposing changes in the distributional parameter  $v(F_Y)$  between two different time periods (t = 0 and t = 1), the decomposition reads as

$$\hat{\Delta}_{O}^{v} = \underbrace{\overline{X}_{1} \left( \hat{\gamma}_{1}^{v} - \hat{\gamma}_{0}^{v} \right)}_{\text{wage structure effect}} + \underbrace{\left( \overline{X}_{1} - \overline{X}_{0} \right) \hat{\gamma}_{0}^{v}}_{\text{composition effect}}, \tag{1}$$

where  $\hat{\Delta}_O^v$  denotes the overall change in the statistic v. The first term on the right-hand side denotes the wage structure effect,  $\hat{\Delta}_S^v$ , which is obtained by holding the distribution of covariates constant and only modifying the conditional wage structure (represented by the RIF coefficients). The second term denotes the composition effect,  $\hat{\Delta}_X^v$ , which is obtained by holding the conditional wage structure (RIF coefficients) constant and varying the distribution of covariates according to the observed changes between t = 0 and t = 1.

to these original contributions for a more extensive description of the empirical approach.

As Fortin et al. (2011) explain, there may be a bias in the decomposition because the linear specification used in the regression is only a local approximation that does not generally hold for larger changes in the covariates. In particular, the RIF coefficients might change if the distribution of the covariates changes even though the true wage structure remains the same. To circumvent this problem, Fortin et al. (2011) propose to combine the RIF regressions with a reweighting approach, where the counterfactual  $\hat{\gamma}_{01}^{v}$  coefficients are obtained from a RIF regression on the period 0 sample reweighted to mimic the period 1 sample (such that  $plim(\overline{X}_{01}) = plim(\overline{X}_{1})$ ). Taken this adjustment into account, the pure wage structure effect<sup>14</sup> amounts to

$$\overline{X}_1(\hat{\gamma}_1^v - \hat{\gamma}_{01}^v)$$

and the pure composition effect<sup>15</sup> to

$$(\overline{X}_{01}-\overline{X}_0)\,\hat{\gamma}_0^v.$$

Just like in the standard Blinder-Oaxaca decomposition, it is possible to obtain the detailed elements of the wage structure and the composition effects which are attributable to different subsets of the vector of explanatory variables, X. However, in case of the wage structure effect, the detailed elements are not unique and, for categorical variables, depend on the choice of the base category, which has to be taken into account when interpreting the results.

It is important to stress that the decomposition method, similar to alternative decomposition approaches used in the literature (e.g. DiNardo et al., 1996; Fairlie, 2005; Mata and Machado, 2005), relies on the assumption of the invariance of the conditional distribution and therefore ignores general equilibrium effects. For our analysis this implies, e.g., that the collective bargaining wage premium is assumed to be independent of collective bargaining coverage. Moreover, the decomposition takes all covariates as exogenously given and not themselves determined by other factors that might also lead to higher wage inequality. This however implies that a causal interpretation of the estimated effects is not possible.

We use this approach to quantify the contributions of an extensive set of explanatory factors to changes in the wage distribution. These factors include the personal characteristics education (four categories)<sup>16</sup>, age (five categories)<sup>17</sup>, nationality (German versus non-German), and dummies for three types of occupations, which are characterized by predominantly manual, routine, and abstract tasks, respectively (similar to Acemoglu and Autor, 2011). Moreover, we consider a large set of plant characteristics: size as measured by

<sup>&</sup>lt;sup>14</sup>The "naive" wage structure effect can be divided into the pure wage structure effect and the reweighting error. See Fortin et al. (2011) for details.

<sup>&</sup>lt;sup>15</sup>The "naive" composition effect can be divided into a pure composition effect and a component measuring the specification error. The specification error captures the difference between the composition effect estimated using a non-parametric reweighting approach and the linear approximation obtained using the RIF regression.

<sup>&</sup>lt;sup>16</sup>1) Low: no vocational training, no high school; 2) Medium: high school and/or vocational training; 3) High: university or technical college. The fourth category consists of observations with missing educational information.

<sup>&</sup>lt;sup>17</sup>1) 18-25 years; 2) 26-35 years; 3) 36-45 years; 4) 46-55 years; 5) 56-65 years.

total employment (10 categories)<sup>18</sup>, the export status (three categories)<sup>19</sup>, a dummy variable that indicates whether the establishment has a works council, two dummy variables capturing the bargaining regime of the establishment (sector-level and firm level agreement, respectively, where no collective bargaining agreement is the base category), two dummy variables that equal one if the plant has invested in communication or information technology and if the (self-assessed) technology status of the plant is above average compared to other establishments in the same industry, respectively, and categorical information on investment per worker (6 categories)<sup>20</sup>. We also include full sets of two-digit industry and federal state dummies to capture sectoral and regional shifts during our period under study.<sup>21</sup> Finally, in this framework the constant captures that portion of (the change in) wage dispersion that cannot be explained by observables and thus can be interpreted as (change in) residual inequality of the base group.

We apply the decomposition method to changes in overall wage distribution as well as to changes in between- and within-plant wage dispersion. As explained above, for the most part, we conduct the decomposition analysis for the period 1996 to 2010, but turn to the more recent period from 2010 to 2014 in an extension. Likewise, while the main analysis focuses on West Germany, we conduct the decomposition analysis for East Germany in a further extension. For statistical inference, we rely on a bootstrap (200 replications) of the whole decomposition. To account for the correlation of wages within plants, a block bootstrap procedure is applied where all observations within a given plant are resampled.

# 5 Preliminary evidence on changes in the workforce composition and the wage structure

Before discussing the detailed decomposition results of changes in wage dispersion, we provide descriptive evidence on changes in the composition of workers and plants as well as changes in the wage structure related to worker and plant characteristics. These constitute the ingredients, albeit in an unconditional and simplified way, to our decomposition analysis where we quantify their respective contributions to the increase in wage inequality.

 $<sup>^{18}1</sup>$ ) 1–4 employees; 2) 5–9 employees; 3) 10–19 employees; 4) 20–49 employees; 5) 50–99 employees; 6) 100–199 employees; 7) 200–499 employees; 8) 500–999 employees; 9) 1000–4999 employees; 10)  $\geq$  5000 employees

<sup>&</sup>lt;sup>19</sup>1) non-exporters; 2) exporters; 3) establishments with missing export information, which comprises a fairly large number of establishments in the service sector.

<sup>&</sup>lt;sup>20</sup>Five categories refer to the quintiles of this variable as measured in the base year 1996, while the sixth category comprises establishments with missing information on investments.

<sup>&</sup>lt;sup>21</sup>We choose our base category to be a medium-skilled worker, in the age range of 26 to 35, with German nationality, employed in an occupation characterized by mainly routine tasks, employed at an establishment with 200 to 499 employees, which does not export, has no works council, is not covered by a collective bargaining agreement of any sort, has not invested in information and communication technology, does not have a high technology status, is in the bottom quintile of investment per worker, belongs to the construction sector, and is located in North Rhine-Westphalia. With very few exceptions (i.e. collective bargaining, works council, investment in ICT), where the "no"-category seems to be the natural benchmark, these constitute the modal categories of the variables in 1996.

Table 1. Worker Shares, Group Mean Wages, and Wage Dispersion within Groups

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
	Worke	er Shares			$\operatorname{Gro}$	oup Mea	n Wages	and Wa	age Disp	ersion v	within Gro	$_{ m 1ps}$		
			(	verall	Wages	3	Betw	een-P	lant W	ages	Wit	hin-Pl	ant Wa	ges
	1996	2010	199	96	20	10	199	96	20	10	199	96	20	10
Worker-Level Characteristics			mean	$_{\mathrm{sd}}$	mean	$\operatorname{sd}$	mean	$_{\mathrm{sd}}$	mean	$\operatorname{sd}$	mean	$\operatorname{sd}$	mean	$_{\rm sd}$
Education: missing	0.07	0.14	4.29	0.42	4.24	0.51	4.34	0.35	4.27	0.45	-0.05	0.22	-0.03	0.26
Education: low	0.15	0.11	4.31	0.28	4.29	0.40	4.42	0.22	4.39	0.37	-0.11	0.19	-0.10	0.21
Education: medium (base)	0.71	0.63	4.49	0.29	4.55	0.37	4.48	0.22	4.56	0.30	0.01	0.21	0.00	0.24
Education: high	0.08	0.12	4.82	0.21	4.95	0.29	4.67	0.18	4.81	0.24	0.15	0.20	0.14	0.23
Age: 18-25	0.08	0.07	4.17	0.29	4.12	0.41	4.35	0.28	4.33	0.42	-0.18	0.21	-0.21	0.27
Age: 26-35 (base)	0.33	0.20	4.42	0.29	4.40	0.41	4.46	0.24	4.47	0.38	-0.03	0.19	-0.07	0.22
Age: 36-45	0.28	0.29	4.53	0.31	4.58	0.41	4.50	0.23	4.55	0.34	0.03	0.20	0.03	0.23
Age: 46-55	0.21	0.31	4.58	0.30	4.61	0.42	4.53	0.21	4.57	0.34	0.05	0.21	0.04	0.23
Age: 56-65	0.10	0.13	4.55	0.34	4.59	0.43	4.50	0.24	4.55	0.35	0.05	0.23	0.04	0.25
Foreign citizenship: no (base)	0.90	0.92	4.50	0.31	4.54	0.43	4.49	0.23	4.54	0.35	0.01	0.21	0.01	0.25
Foreign citizenship: yes	0.10	0.08	4.30	0.36	4.32	0.48	4.39	0.32	4.39	0.44	-0.08	0.20	-0.07	0.23
Occupation group: manual	0.05	0.06	4.21	0.38	4.23	0.43	4.26	0.35	4.29	0.39	-0.05	0.21	-0.05	0.24
Occupation group: routine (base)	0.76	0.74	4.44	0.29	4.47	0.41	4.47	0.22	4.49	0.35	-0.03	0.20	-0.03	0.23
Occupation group: abstract	0.19	0.20	4.72	0.28	4.82	0.39	4.59	0.21	4.71	0.30	0.12	0.22	0.11	0.27
Plant-Level Characteristics														
Plant size: 1–4	0.05	0.04	4.17	0.42	4.09	0.55	4.17	0.40	4.09	0.53	0.00	0.12	0.00	0.16
Plant size: 5–9	0.07	0.06	4.32	0.36	4.28	0.45	4.32	0.31	4.28	0.40	0.00	0.19	0.00	0.23
Plant size: 10–19	0.09	0.08	4.36	0.32	4.38	0.42	4.36	0.24	4.38	0.35	0.00	0.21	0.00	0.24
Plant size: 20–49	0.15	0.16	4.42	0.30	4.44	0.40	4.42	0.20	4.44	0.33	0.00	0.22	0.00	0.24
Plant size: 50–99	0.11	0.12	4.48	0.31	4.49	0.40	4.48	0.21	4.49	0.30	0.00	0.23	0.00	0.27
Plant size: 100–199	0.10	0.14	4.51	0.29	4.50	0.44	4.51	0.17	4.50	0.35	0.00	0.23	0.00	0.26
Plant size: 200–499 (base)	0.17	0.17	4.55	0.27	4.60	0.39	4.55	0.16	4.60	0.30	0.00	0.22	0.00	0.26
Plant size: 500–999	0.08	0.08	4.58	0.26	4.68	0.36	4.58	0.14	4.68	0.25	0.00	0.22	0.00	0.26
Plant size: 1000-4999	0.13	0.10	4.60	0.26	4.80	0.29	4.60	0.14	4.80	0.16	0.00	0.21	0.00	0.24
Plant size: $>=5000$	0.04	0.04	4.68	0.21	4.90	0.22	4.68	0.10	4.90	0.08	0.00	0.18	0.00	0.21
Exporter: missing	0.21	0.13	4.56	0.30	4.66	0.37	4.56	0.20	4.66	0.26	0.00	0.22	0.00	0.26
Exporter: no (base)	0.46	0.50	4.40	0.34	4.40	0.46	4.40	0.26	4.40	0.40	0.00	0.21	0.00	0.24
Exporter: yes	0.33	0.37	4.55	0.28	4.65	0.36	4.55	0.18	4.65	0.26	0.00	0.22	0.00	0.25
Works council: no (base)	0.37	0.44	4.35	0.35	4.32	0.46	4.35	0.29	4.32	0.38	0.00	0.21	0.00	0.24
Works council: yes	0.63	0.56	4.56	0.27	4.69	0.34	4.56	0.16	4.69	0.24	0.00	0.22	0.00	0.25
Collective agreement: none (base)	0.14	0.34	4.38	0.43	4.43	0.47	4.38	0.37	4.43	0.40	0.00	0.22	0.00	0.26
Collective agreement: firm level	0.11	0.09	4.47	0.33	4.63	0.37	4.47	0.24	4.63	0.28	0.00	0.22	0.00	0.24
Collective agreement: sector level	0.75	0.57	4.50	0.29	4.57	0.41	4.50	0.20	4.57	0.34	0.00	0.21	0.00	0.24
Investment in ICT: no (base)	0.41	0.44	4.40	0.33	4.41	0.46	4.40	0.26	4.41	0.39	0.00	0.21	0.00	0.24
Investment in ICT: yes	0.59	0.56	4.53	0.30	4.62	0.39	4.53	0.21	4.62	0.31	0.00	0.22	0.00	0.25
High technological status: no (base)	0.79	0.81	4.48	0.32	4.52	0.44	4.48	0.24	4.52	0.36	0.00	0.22	0.00	0.25
High technological status: yes	0.21	0.19	4.50	0.32	4.55	0.43	4.50	0.24	4.55	0.36	0.00	0.21	0.00	0.24
Investment per worker: missing	0.07	0.06	4.51	0.30	4.67	0.42	4.51	0.22	4.67	0.35	0.00	0.21	0.00	0.24
Investment per worker: 1st quintile (base)	0.19	0.30	4.42	0.35	4.39	0.48	4.42	0.27	4.39	0.41	0.00	0.21	0.00	0.25
Investment per worker: 2nd quintile	0.19	0.22	4.45	0.33	4.51	0.41	4.45	0.25	4.51	0.33	0.00	0.23	0.00	0.25
Investment per worker: 3rd quintile	0.19	0.15	4.48	0.30	4.55	0.38	4.48	0.21	4.55	0.29	0.00	0.22	0.00	0.25
Investment per worker: 4th quintile	0.19	0.15	4.52	0.30	4.63	0.39	4.52	0.22	4.63	0.31	0.00	0.21	0.00	0.24
Investment per worker: 5th quintile	0.19	0.12	4.53	0.31	4.65	0.38	4.53	0.23	4.65	0.30	0.00	0.20	0.00	0.23

Notes: Analysis based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany. Sampling weights are employed. We construct the measure of between-plant (within-plant) wages by using yearly regressions of log individual wages on a full set of plant fixed effects. We then take the predicted (residual) wages as a measure of between-plant (within-plant) wages. Base categories of all binary / categorical variables in the subsequent RIF regressions are indicated in parentheses in the first column.

#### 5.1 Changes in the composition of workers and plants

The first two columns of Table 1 illustrate the composition of workers according to various individual and plant characteristics for the years 1996 and 2010.

In terms of sociodemographic characteristics, there is a visible trend towards more highly skilled and, even more so, older workers. The share of workers with university education in our sample increased from 8 percent in 1996 to 12 percent in 2010.<sup>22</sup> Also, the share of workers in the age group 46–55 (56–65) increased from 21 percent (10 percent) to 31 percent (13 percent). In contrast, there are small declines in the shares of routine workers and foreign workers, respectively. It has to be noted, however, that in the present data, workers are classified as foreigners/natives based on their nationality. Since the German nationality law was reformed during our sample period, making it easier to obtain German citizenship, this decline most likely reflects changes in citizenship rather than a decline in the number of migrant workers.

In terms of plant characteristics, the most drastic change relates to collective bargaining coverage. Table 1 shows that the share of workers covered by a sector-level bargaining agreement declined by 18 percentage points (from 75 percent to 57 percent), which was compounded by a small decrease in the share of workers covered by firm-level bargaining agreements (from 11 percent to 9 percent).<sup>23</sup> Note that, since we are considering an unbalanced panel of plants, this decline comes about by both previously covered plants leaving collective bargaining and entering (young) plants being less likely to follow a collective agreement than exiting (old) ones. As a further change to the structure of industrial relations, the share of workers in plants with a works council also declined.

In addition, there has a be a shift towards establishments with less investment per worker. Finally, regarding the importance of international trade, no clear pattern emerges as both the share workers at exporters and non-exporters increased in our sample, at the expense of establishments with missing information on exports. Most likely, however, the group with missings (which mostly are in the service sector) will predominantly consist of non-exporters.

## 5.2 Changes in the wage structure relating to worker and plant characteristics

The second part of Table 1 displays the structure and development of between-group mean wages and intra-group wage dispersion (as measured by the standard deviation), respectively, where these groups are again formed according to the same worker and plant characteristics. In addition to overall wages, group-mean wages and intra-group wage dispersion

<sup>&</sup>lt;sup>22</sup>In addition, the share of workers with missing education information also increased. According to their (unconditional) mean wages, this group seems to resemble most closely the group of low-skilled workers (which decreased by an amount similar to the increase of the missings), suggesting that particularly the share of medium-skilled workers declined.

<sup>&</sup>lt;sup>23</sup>In Germany, the recognition of trade unions regarding collective bargaining purposes is at the discretion of the firm. Once a firm has recognized a union, collective bargaining outcomes apply de facto to all workers in that firm, regardless of whether they are union members or not (for a discussion see e.g. Dustmann et al., 2009 and Fitzenberger et al., 2013). Such collective agreements are either formed at the firm or at the sector level. Firms that once have recognized a collective agreement, however, can later decide to opt out at their own discretion.

are separated into their between-plant and within-plant components, which have been obtained as predicted values and residuals, respectively, of year-specific regressions of log real wages on a full set of plant fixed effects.

#### 5.2.1 Intra-group wage dispersion

We first focus on the structure and development of intra-group wage dispersion, i.e. on the columns displaying the group-specific standard deviations of wages, and start with overall wages (columns 5 and 7). In this respect, the table portrays two main findings. First, intra-group wage dispersion differs markedly across groups. For example, regarding individual characteristics, it slightly increases in the workers' age, and it is larger for foreigners than for natives. Surprisingly, it seems to decline rather quickly with education. With respect to plant characteristics, it is, not surprisingly, substantially larger among plants not covered by collective bargaining agreements and among plants without a works council. It is also larger among smaller plants and non-exporters than among their respective counterparts.

Thus, several of the important compositional changes outlined in the previous subsection, in particular those regarding age, collective bargaining coverage and the existence of a works council, entail a relative shift towards groups with larger within-group wage dispersion, suggesting that composition effects should play a role for the increase in wage inequality.

Second, in all groups, with no single exception, intra-group wage dispersion increased markedly over the period of analysis. Thus, in addition to composition effects, wage structure effects have also played a role. The magnitude of this increase again differs across groups, sometimes reenforcing initial differences in intra-group wage dispersion (e.g. in the case of plant size where it increased more among small than among large plants) and sometimes dampening them (e.g. in the case of collective bargaining where intra-group wage dispersion increased more among covered than among uncovered plants).

Focusing on the structure and development of between- and within-establishment wage dispersion, the between-plant component is larger than the within-component for most subgroups.<sup>24</sup> There are some differences, however. For example, among workers employed at larger plants, the within component is more important. The same goes for workers employed at plants with a works council. In addition, the between-plant component has grown more strongly over time for most subgroups.

#### 5.2.2 Mean wage gaps between groups

The overall wage structure is not only shaped by wage dispersion within groups but also by (mean) wage gaps between groups.

Note that these mean differences matter for both the composition effect and the wage structure effect of the decomposition analysis. To the extent that between-group wage

<sup>&</sup>lt;sup>24</sup>Note, however, that between-establishment and within-establishment wage dispersion, as measured by the variance, do not have to add up to the total for every single subgroup as they are still based on the plant-mean wages and within-plant wage residuals that we calculated for the entire sample. The covariance between these two terms will be zero if subgroups are formed according to plant-level characteristics – where the mean within-group wage residual is always zero by construction – but will generally not be equal to zero if subgroups are formed according to individual characteristics.

differentials change, they will contribute to the wage structure effect. On the other hand, to the extent that there are compositional shifts towards groups whose (initial) group-mean wages are relatively far from (close to) the grand mean, these will contribute to greater (lower) wage inequality via the composition effect.

Table 1 also shows mean wages by subgroups. At the individual level, we can observe a strong increase in the wage gap between the highly educated and those with lower levels of education and in the "returns" to an occupation characterized by abstract tasks relative to routine and manual tasks. There is also a growing wage penalty for the younger age groups. In addition, wage differences increased along a number of plant characteristics, such as plant size, exporting, the existence of a works council, and investment in ICT. Again, we also show separately the structure and development of between-plant and within-plant mean wages.<sup>25</sup> Interestingly, we see that, both in the education and occupation dimension, most of the increase in the between-group wage gaps are due to the between-plant component, providing some tentative evidence that sorting in these dimensions has become more important over time.

### 6 Decomposition results

We now turn to our detailed decomposition results based on RIF regressions. Our main specification generally refers to West Germany and focuses on the change in wage inequality between 1996 and 2010. We first discuss our findings regarding overall wage inequality. We then turn to our separate decomposition results for between-plant and within-plant wage dispersion and, in further extensions, explore differences between lower-tail and upper-tail wage dispersion, changes over time, and differences between West and East Germany.

## 6.1 Baseline decomposition of the change in overall wage inequality

To ease the inspection of the results and the comparison across the different factors in terms of their relative importance for the rise in wage inequality, we depict the decomposition results graphically (Figure 2). The bars show the composition and wage structure effects, respectively, associated with the different sets of variables and the capped spikes the associated 95% confidence intervals, which have been calculated based on the bootstrapped standard errors. The tables with the full set of decomposition results including the standard errors as well as the specification and reweighting errors are shown in the Appendix.

Looking first at the total composition and wage structure effects, respectively, reveals that the former contribute about 25 percent and the latter about 75 percent to the increase in wage dispersion over the sample period. Among the composition effects, the ones associated with collective bargaining coverage contribute the most to the increase in wage dispersion. This reflects the strong decline in (particularly sector-level) collective bargaining coverage rates discussed in Section 5. As shown in the same section, this decline supposes

 $<sup>^{25}</sup>$ Due to the aforementioned reason that mean within-plant wage residuals are zero by construction at the plant level, this distinction is only interesting for groupings defined according to individual-level as opposed to plant-level characteristics.

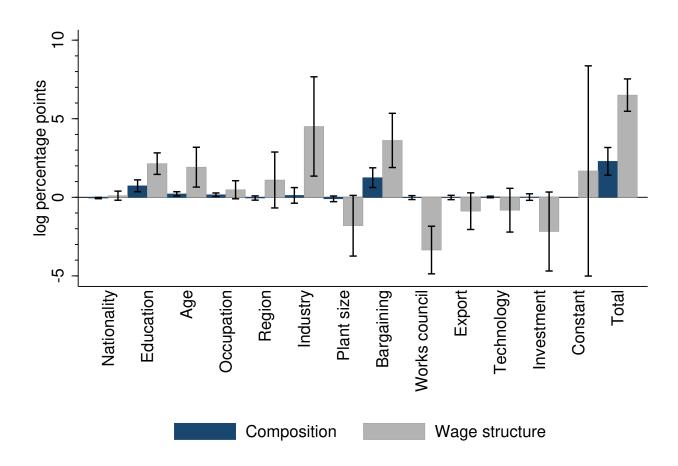


Figure 2. Baseline Results: Decomposition of the Change in the Overall Variance, 1996–2010

Notes: Figure 2 shows the decomposition results of the change in the variance of log wages between 1996 and 2010. The bars show the composition and wage structure effects associated with the different sets of variables and the capped spikes the corresponding 95% confidence intervals. The latter are calculated based on bootstrapped standard errors (200 replications of the entire procedure accounting for clustering at the plant level). The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany.

a relative shift towards the group of (uncovered) workers which is characterized by both higher intra-group wage dispersion and group-mean wages that are relatively far from the grand mean. The contribution of the bargaining-related composition effect amounts to 1.25 log percentage points, which corresponds to 14.4 percent of the total increase and more than half of the total composition effect, respectively. Among the remaining composition effects, only shifts in the education profile of workers have played a small, but non-negligible role, contributing 0.7 log percentage points to the rise in wage inequality. They capture the relative shifts towards higher-educated workers, i.e. a group characterized by group-mean wages that are relatively far from the grand mean (cf. Section 5.2.1).

Turning to the wage structure effects, the ones associated with industry identifiers and, once more, collective bargaining are the quantitatively most important ones (4.51 and 3.62 log percentage points, respectively). Recall that the wage structure effects capture both a between component, that is changes in wage differentials between groups (e.g. industries, different bargaining regimes), and a within component, that is changes in wage dispersion

within groups (compared to the base group). In the case of collective bargaining, both of these components are at work and contribute to greater wage dispersion. On the one hand, the wage gap between covered and uncovered workers increased slightly, and on the other hand, wage dispersion within the group of workers covered by (sector-level) agreements rose much more strongly than among covered ones, our base group (cf. Subsection 5.2). The latter development has also been highlighted by Dustmann et al. (2014) and is related to an increasing flexibility within collective agreements. A similar story applies to the industry-related wage structure effect which captures both increasing industry mean wage differentials and a growing wage dispersion within industries. While the RIF-based decomposition result does not allow us to disentangle the two, the latter channel seems to be the more important one. That is, if we do the same simple decomposition of the log wage variance into a between and a within component as in Section 3, but this time focus on industries rather than plants, it turns out that about 70 percent of the increase in wage inequality over our period of analysis took place within as opposed to between industries.

Among the remaining wage structure effects, the ones relating to education and age contribute positively to rising wage dispersion, while the ones associated with the existence of a works council, investment per worker, and plant size dampen it, although the latter two are not (or only barely) statistically significant. The other wage structure effects are not important determinants of greater wage dispersion.<sup>26</sup>

## 6.2 Decomposition of changes in between-plant and withinplant wage inequality

We now separately decompose changes in between-plant and within-plant wage dispersion. For this purpose, we apply the same decomposition technique to changes in the variance of predicted wages and wage residuals, respectively, of a regression of log individual wages on a full set of plant fixed effects. At first sight, a natural expectation could be that plant characteristics, with their composition and wage structure effects, should be the main drivers of between-plant wage dispersion while individual characteristics should be the main drivers of within-plant wage dispersion. However, that does not need to be the case. To the extent that individual characteristics also matter for between-plant wage inequality, this suggests that workers with different characteristics are unevenly distributed across plants, providing (indirect) evidence for assortative matching. Indeed, previous research has already shown the growing importance of assortative matching, as measured by the correlation between individual and plant effects, for wage inequality (Card et al., 2013). On the other hand, to the extent that establishment characteristics matter for within-establishment wage dispersion, this suggests that these characteristics affect individual workers' wages unevenly.

We first turn to the detailed decomposition results of between-plant wage inequality, shown in the left panel of Figure 3 (and Table 3 in the Appendix). As the increase in the

<sup>&</sup>lt;sup>26</sup>This includes the wage structure effect related to exporting. The latter result stands in contrast to the one obtained by Baumgarten (2013) who however focused on the manufacturing sector only and considered a slightly different sampling period – the analysis of Baumgarten (2013) ends in 2007, that is before the exporter wage premium decreased during the Great Recession (see Dauth et al., 2015).

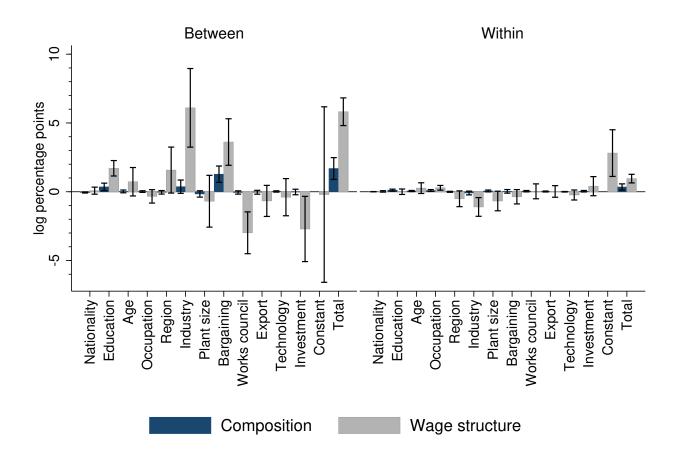


Figure 3. Decomposition of Changes in the Between-Plant and the Within-Plant Variance, 1996–2010

Notes: The between-plant (within-plant) variance is constructed as the variance of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The bars show the composition and wage structure effects associated with the different sets of variables and the capped spikes the corresponding 95% confidence intervals. The latter are calculated based on bootstrapped standard errors (200 replications of the entire procedure accounting for clustering at the plant level). The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany.

between-plant variance accounts for the largest part of the total increase, it is not surprising that the main factors contributing to the rise are identical. Again, most of the increase (roughly 80 percent) is due to wage structure effects. Among the composition effects, the largest contribution to the increase in between-plant wage inequality again comes from changes in collective bargaining coverage rates. The bargaining-related composition effect amounts to 1.27 log percentage points (corresponding to 18 percent of the total increase in between-plant wage inequality or 75 percent of the total composition effect) and is, thus, even slightly larger than its contribution to overall inequality, both in relative and absolute terms. Thus, the decline in collective bargaining, driven primarily by a strongly decreasing share of plants covered by sector-level agreements, has been associated with a greater dispersion of wages across plants. Among the composition effects related to individual characteristics, (only) the explanatory factor education contributes non-negligibly to the rise in between-plant wage dispersion. The latter's contribution amounts to 0.35 log percentage points, corresponding to 5 percent of the total increase in between-plant wage inequality or

21 percent of the total composition effect.

When it comes to the wage structure effects, the ones associated with the industry and the collective bargaining regime again contribute quantitatively the most to increasing between-plant wage inequality. In contrast, the wage structure effects associated with the existence of a works council and the level of investment per worker are negative, reflecting that between-plant wage dispersion has increased less among plants with a works council than among the ones without (the base group) and has also declined within a given investment category relative to the base group (the bottom quintile of investment per worker). Among the wage structure effects associated with worker-level variables, it is again the one relating to education that stands out in contributing to greater between-plant wage inequality. The education-related wage structure effect mainly captures that plant-level wage differentials between education groups have increased. That is, the gap between the mean plant wage of a high-skilled and a low-skilled worker and between a high-skilled and one with missing information on education has increased substantially over time (by 17 and 21 log percentage points, respectively). This is consistent with the notion of increased assortative matching along the skill dimension, where high-skilled workers are more and more concentrated at high-wage paying plants and low-skilled workers at low-wage paying plants. This result is in line with Card et al. (2013) who also find that the degree of sorting of different education and occupation groups to different establishments has risen in West Germany.<sup>27</sup>

We now turn to the results on within-plant wage inequality. The most striking finding is that by far the largest contribution to the increase in this subcomponent of wage inequality comes from the wage structure effect associated with the constant, which captures the increase in residual inequality of the base group. In fact, the latter is twice as large as the total observed increase in within-plant inequality, implying that all remaining factors have, in sum, had a dampening effect.

If we look at those factors separately, only few are statistically significant and/or noteworthy in terms of their magnitude. One of them is occupation, which contributes positively and significantly to increased within-plant wage inequality both in terms of the composition and the wage structure effect. Recall that we have grouped occupations in terms of their task characteristics, distinguishing predominantly manual, routine (the base group), and abstract occupations. The composition effect reflects the relative decrease in the share of routine occupations which are characterized by lower within-plant wage dispersion and mean (plant-residualized) wages closer to the grand mean. The occupation-related wage structure effect, in turn, arises mainly from greater increases in within-plant wage dispersion among manual and, in particular, abstract occupations relative to routine ones. Among the remaining individual-level characteristics, compositional shifts towards a larger share of high-educated workers have also led to higher within-plant wage inequality.

Interestingly, the industry-related wage structure effect, the single most important factor for increased between-plant wage dispersion, contributes negatively to within-plant wage dispersion. Since there are no differences across industries in terms of their mean within-

<sup>&</sup>lt;sup>27</sup>We assume that workers with missing educational information are most likely low skilled workers. According to their unconditional mean wages, this is a plausible assumption, see Table 1.

plant wages – they are zero by construction – this is due to a relatively smaller increase in within-plant wage dispersion among industries other than the base industry, i.e. construction. In addition, collective bargaining, which was another main factor for increased between-plant wage dispersion does not matter at all for changes in within-plant wage dispersion.

In summary, this analysis shows that the main drivers of between-plant and within-plant wage dispersion differ and some explanatory factors even are related to both subcomponents of wage inequality in opposing ways. The most important drivers of the large increase in between-plant wage inequality have been the wage structure effects associated with the industry and the collective bargaining regime as well as the compositional shift implied by the strong decline in collective bargaining coverage. The worker-level characteristic education is the only one where both the composition and wage structure effects are positively related to both subcomponents of wage dispersion. Interestingly, the wage structure effect associated with education is quantitatively more important for between-plant than for within-plant wage inequality. This mirrors the finding that most of the increase in the skill wage gap arises from an increase in between-plant rather than within-plant wage differentials, reflecting increased assortative matching along the skill dimension (in line with Card et al., 2013).

#### 6.3 Top vs bottom

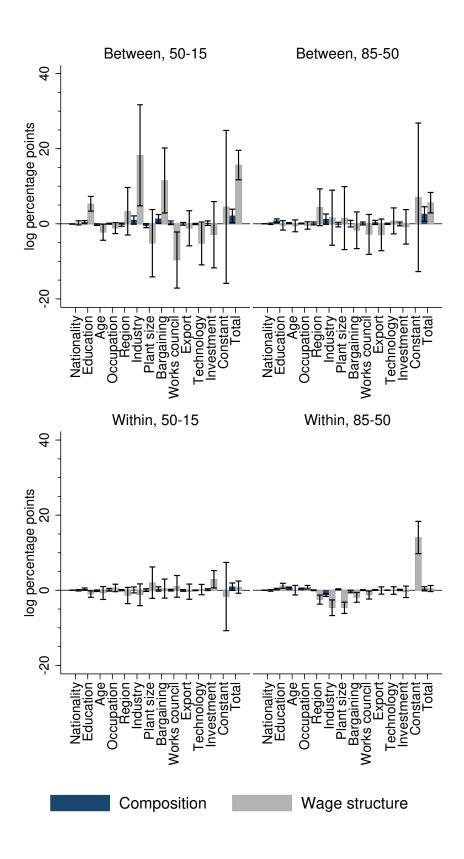
Although the log wage variance has the advantage that the between-plant and the within-plant components add up to the total, it does not allow distinguishing sources of wage dispersion at the top and the bottom of the wage distribution. Therefore, we also do our decomposition analysis for the the 50–15 log wage differential (as a measure of lower-tail wage inequality) and the 85–50 log wage differential (as a measure of upper-tail wage inequality) of both mean plant wages and within-plant wage residuals, respectively.<sup>28</sup> Results are shown in Figure 3 (and Table 4 in the Appendix).

As far as between-plant wage inequality is concerned, more than two thirds of the increase in wage dispersion over the period of analysis (18.5 of 26.8 log percentage points) occurred at the lower part of the wage distribution. This difference between lower-tail and upper-tail inequality is due to wage structure effects, while composition effects are, in sum, small and of about equal magnitude. The main driving forces of the increase in lower-tail between-plant wage dispersion are the wage structure effects related to the industry and the collective bargaining regime, which amount to 18.2 and 11.5 log percentage points, respectively. In contrast, both of these factors do not matter at all for the change in upper-tail between-plant wage dispersion, where the wage structure effects associated with the region and the constant are quantitatively the most important ones.<sup>29</sup>

The composition effect associated with collective bargaining is again only relevant for lower-tail wage inequality. Thus, the decline in collective bargaining has been associated with a widening of the lower part of the plant wage distribution, where union wages are of

<sup>&</sup>lt;sup>28</sup>Note that, now, the between-plant and the within-plant component of any inequality measure do not anymore (necessarily) add up to the total.

<sup>&</sup>lt;sup>29</sup>Note that the constant is not statistically significant.



**Figure 4.** Decomposition of Changes in Between-Plant and Within-Plant Quantile Differences, 1996-2010

Notes: The between-plant (within-plant) quantile differences are constructed as percentile differences (50-15 and 85-50, respectively) of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The bars show the composition and wage structure effects associated with the different sets of variables and the capped spikes the corresponding 95% confidence intervals. The latter are calculated based on bootstrapped standard errors (200 replications of the entire procedure accounting for clustering at the plant level). The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany.

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course more likely to bind than in the upper part of the distribution.

The picture looks different for within-plant wage inequality, where about 60 percent of the (small) increase in total wage dispersion over the sample period took place in the upper half of the wage distribution (1.96 of 3.31 log percentage points). By far, the main source of this increase in upper-tail within-plant wage dispersion is not related to any particular factor but to the wage structure effect of the constant, which captures an increase in residual inequality of the base group. The contribution of the constant amounts to 14 log percentage points, which is seven (!) times bigger than the total change in this inequality measure. Further contributions, which are statistically significant and positive but small, come from the explanatory factors education, occupation – both through the composition and the wage structure effects – and age, where only the composition effect is relevant. In contrast, wage structure effects associated with the region, the industry, plant size, the collective bargaining regime, and the existence of a works council all have negative (i.e. inequality-dampening) effects.

Finally, regarding the change in lower-tail within-plant wage dispersion, hardly any results stand out, the main exception being the wage structure effect related to investment per worker, which is statistically significant and amounts to 2.9 log percentage points. Thus, increases in wage dispersion within plants in higher quintiles of investment per worker (and the missing category) were a main factor behind the (modest) increase in lower-tail within-plant wage inequality, which would be consistent with the notion that these investments favored some workers and hurt others within the same plant, possible as a consequences of technological or organizational change.

#### 6.4 The recent decline in wage inequality

So far, we have analyzed the contributions of the different factors to the change in wage dispersion over the period 1996 to 2010, which was characterized by a pronounced and fairly steady increase in wage inequality. Thereafter, however, rising wage dispersion seems to have come to a halt. In this subsection, we conduct the same decomposition analysis for the change in wage inequality between 2010 and 2014 to obtain a better understanding of the change in the inequality dynamics. We again do so separately for changes in between-plant and within-plant wage dispersion. Results are displayed in Figure 5 (and Table 5 in the Appendix, where we also list the decomposition results for the change in the overall variance).

In the following, we highlight a few noteworthy findings. First of all, the decline in the log wage variance has been very modest (0.47 log percentage points) and has been entirely due to the between-plant component, while within-plant wage dispersion continued to rise slightly. Interestingly, for all our wage dispersion measures, the total composition effects are positive (i.e. inequality-increasing) while the total wage structure effects have a dampening effect on inequality. This result, however, has to been interpreted with some caution. Due to a change in the compulsory notifications of employers to the social security agencies implemented for employment spells ending after November 30, 2011, the set of available variables and their exact definitions in the administrative records used in our analysis changed during the most recent time interval. As a consequence, the share of missings, in

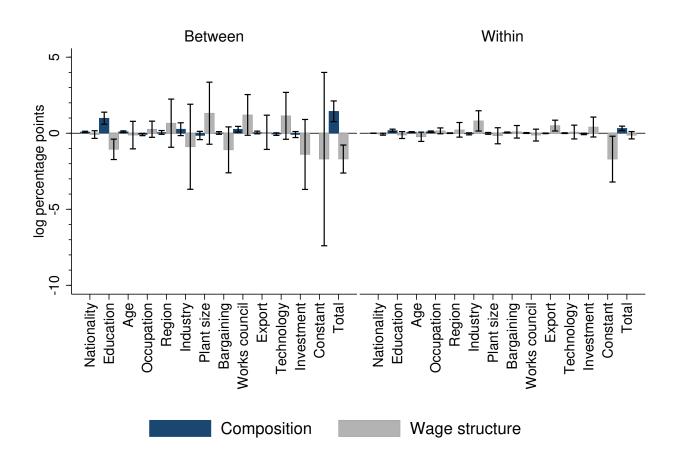


Figure 5. Decomposition of Changes in the Between-Plant and the Within-Plant Variance, 2010–2014

Notes: The between-plant (within-plant) variance is constructed as the variance of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The bars show the composition and wage structure effects associated with the different sets of variables and the capped spikes the corresponding 95% confidence intervals. The latter are calculated based on bootstrapped standard errors (200 replications of the entire procedure accounting for clustering at the plant level). The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany.

particular regarding the education variable, increased sharply (from 14 to 28 percent, mostly at the expense of low-skilled and medium-skilled workers). This implies a seeming change in the composition of the workforce, which is entirely data-driven, but clearly affects the decomposition results. Indeed, the spurious education-related composition effect is positive, statistically significant, and quantitatively the most important one for all the measures of wage dispersion. Likewise, the education-related wage structure effect, which is negative and substantial for the change in the between-plant variance, is rather misleading as the apparent "returns" to, e.g., missing education were severely altered due to the large increase in missings.

Regarding the change in the between-plant wage variance, wage structure effects associated with the constant, investment per worker, the collective bargaining regime, the level of education (see above), and the industry contribute the most to declining wage dispersion in terms of the point estimate, but none of them is statistically significant. Still, apart from investment, which had a dampening effect already in the earlier period, and the constant,

all of the other mentioned factors were important drivers of the increase in between-plant wage dispersion between 1996 and 2010. Thus, while some of the most important drivers of between-plant wage inequality remain the same, the direction of their influence changed, turning from inequality-increasing to inequality-dampening.

This is not true regarding the slight increase in within-plant wage dispersion. Here, the wage structure effects associated with the industry and exporting are statistically significant and quantitatively the most important ones, which constitutes a change with respect to the earlier period. While exporting did not play a role at all in the period 1996 to 2010, the industry wage structure effect was negative. Since the wage structure effect of plant-level variables captures differential changes in within-group wage dispersion relative to the base category, this implies that, compared to the construction industry (the base category), within-plant wage dispersion in the remaining industries was rising by less in the earlier period, but by more in the years 2010 to 2014.

#### 6.5 Wage inequality in East Germany

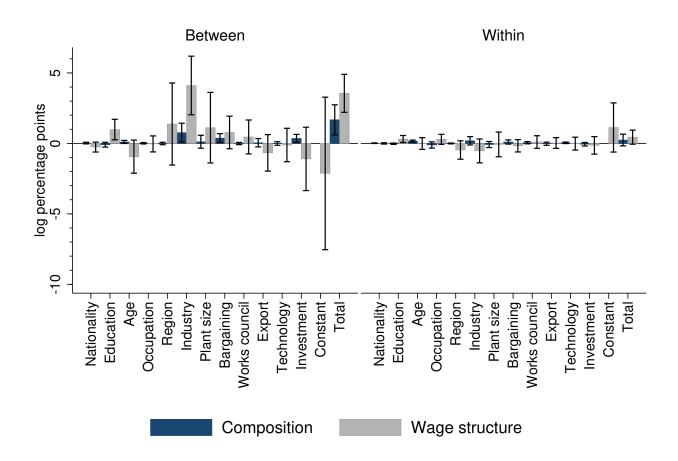
Our main analysis focused on West Germany to allow for a better comparison of our results with seminal earlier papers on the topic (Dustmann et al., 2009; Card et al., 2013). Furthermore, since the labor markets and wage schedules in West and East Germany differ markedly – even today, but particularly in the 1990s – pooling both regions would likely have contaminated the decomposition results. In this subsection, we briefly report on the decomposition results for East Germany. We focus on our main period of analysis, 1996 to 2010. Results are displayed in Figure 6 (and Table 6 in the Appendix).

We focus on a few notable similarities and differences with respect to West Germany. First of all, the increase in wage dispersion has been smaller than in the West (5.1 as opposed to 8.7 log percentage points in terms of the total variance, starting from a slightly higher initial level of inequality). Yet the relative importance of the between-plant and the within-plant component to the total increase has been similar, with the former's contribution amounting to 86 percent. Like in the West, the industry-related wage structure effect is the most important driver of total and between-plant wage dispersion. In addition, shifts in the industry structure of employment (i.e. the composition effect) also contributed towards higher inequality, which was not the case in the West. In contrast, while (the decline in) collective bargaining does also matter in terms of the composition effect, the bargaining-related wage structure effect is not a factor behind the increase in wage dispersion in the East. As far as other explanatory factors are concerned, changes in the education-related wage structure are an even more important driver of wage dispersion relative to the West, which holds particularly true for changes in within-plant wage dispersion.

In sum, however, despite the aforementioned differences, the dynamics of wage dispersion and its main sources have been remarkably similar in West and East Germany.

### 7 Summary and conclusion

Like many other countries, Germany experienced a strong increase in wage dispersion in the last few decades before coming to a halt after 2010. Much of this increase took place between



**Figure 6.** Decomposition of Changes in the Between-Plant and the Within-Plant Variance in East Germany, 1996–2010

Notes: The between-plant (within-plant) variance is constructed as the variance of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The bars show the composition and wage structure effects associated with the different sets of variables and the capped spikes the corresponding 95% confidence intervals. The latter are calculated based on bootstrapped standard errors (200 replications of the entire procedure accounting for clustering at the plant level). The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in East Germany.

as opposed to within establishments, in line with an increasing international evidence.

In this paper, we have used rich linked employer-employee data and applied a detailed decomposition analysis based on recentered influence function (RIF) regressions to identify the sources of this increase in wage dispersion in Germany. In doing so, we have paid particular attention to the importance of many different plant characteristics and to the divergent sources of between-plant and within-plant wage dispersion, respectively.

Our main decomposition results point to shifts in the industry-related wage structure, the decline in collective bargaining coverage, and changes in the bargaining-related wage structure, both through a small increase in the wage gap between covered and uncovered plants and a strong increase in wage dispersion within the group of covered establishments, as main drivers of the increase in wage inequality. These factors affected primarily between-plant as opposed to within-plant and lower-tail as opposed to upper-tail wage dispersion. Among the individual-level variables, education matters the most, where both employment

shifts towards more highly skilled workers and, even more so, changes in the skill-related wage structure have played important roles. The education-related effect is quantitatively more important for between-plant than for within-plant wage inequality, reflecting increased sorting of workers along the skill dimension. In contrast, several other plant-level characteristics, including plant size, the exporting status, plant technology, and investment per worker are all of little if any quantitative importance for the increase in wage dispersion.

It is important to note, however, that, while the decomposition analysis has enabled us to identify the proximate sources of increased wage dispersion between and within plants, we are not able to attach to them a causal interpretation in a deeper, structural sense. For example, changes in the industry-related and the bargaining-related wage structure did not come about exogenously. It is perfectly conceivable that these have been caused by changes in the competitive environment, potentially induced, e.g., by an accelerated globalization.<sup>30</sup> Therefore, relating the proximate sources of rising wage inequality identified in our analysis to deeper structural causes is a high priority for future research.

 $<sup>^{30}</sup>$ Dustmann et al. (2014) indeed suggest that rising opportunities to offshore production induced by the fall of the iron curtain contributed to a rising flexibilization of wages within the covered sector.

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## Appendix

Table 2. Decomposition of Changes in the Overall Variance, 1996–2010

Total change	8.68*** [0.47]				
	Composition	Wage structure			
Nationality	-0.05**	0.10			
	[0.02]	[0.15]			
Education	0.73***	2.14***			
	[0.19]	[0.35]			
Age	0.22***	1.92***			
	[0.07]	[0.65]			
Occupation	0.16***	0.48			
	[0.06]	[0.29]			
Region	-0.05	1.10			
	[0.07]	[0.91]			
Industry	0.12	$4.51^{***}$			
	[0.25]	[1.61]			
Plant size	-0.10	-1.81			
	[0.09]	[0.99]			
Collective bargaining	1.25***	3.62***			
	[0.32]	[0.88]			
Works council	-0.02	-3.36***			
	[0.06]	[0.77]			
Export	-0.01	-0.88			
	[0.07]	[0.60]			
Technology	0.02	-0.82			
	[0.03]	[0.71]			
Investment per worker	0.01	-2.18*			
	[0.11]	[1.28]			
Constant		1.68			
		[3.41]			
Total	2.29***	6.50***			
	[0.45]	[0.53]			
Reweighting error		0.07			
	[(	0.19]			
Specification error	_	0.04			
•		2.001			

Notes: The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany. Sampling weights are employed. All numbers are given in log percentage points. Bootstraped standard errors (200 replications of the entire procedure) account for clustering at the plant level and are shown in brackets. Asterisks indicate statistical significance at the 1%(\*\*\*), 5%(\*\*), or 10%(\*) level.

[0.23]

Table 3. Decomposition of Changes in the Between-Plant and the Within-Plant Variance, 1996–2010

	Between-p	olant variance	Within-plant variance			
Total change		26***	1.41***			
	[0.46]		[0.13]			
	Composition	Wage structure	Composition	Wage structure		
Nationality	-0.05***	0.08	0.01	0.03		
	[0.02]	[0.13]	[0.00]	[0.03]		
Education	$0.35^{**}$	1.71***	$0.12^{***}$	0.00		
	[0.14]	[0.29]	[0.04]	[0.10]		
Age	0.02	0.73	0.05	0.26		
~	[0.05]	[0.53]	[0.02]	[0.20]		
Occupation	0.01	-0.34	0.09***	0.29***		
-	[0.03]	[0.25]	[0.03]	[0.09]		
Region	-0.04	1.58*	0.00	-0.51		
	[0.07]	[0.85]	[0.02]	[0.29]		
Industry	[0.37]	6.10***	-0.09	-1.11***		
v	[0.25]	[1.46]	[0.07]	[0.35]		
Plant size	-0.16	-0.69	[0.06]	-0.67		
	[0.12]	[0.96]	[0.03]	[0.36]		
Collective bargaining	1.27***	3.61***	[0.03]	-0.36		
	[0.30]	[0.86]	[0.07]	[0.27]		
Works council	-0.05	-2.99****	0.04	[0.03]		
	[0.06]	[0.78]	[0.03]	[0.28]		
Export	-0.04	-0.67	[0.02]	[0.02]		
•	[0.07]	[0.58]	[0.02]	[0.22]		
Technology	[0.02]	-0.40	[0.00]	-0.24		
O.	[0.02]	[0.69]	[0.01]	[0.19]		
Investment per worker	-0.02	-2.71**	0.04	0.40		
1	[0.10]	[1.21]	[0.03]	[0.35]		
Constant	. ,	-0.20	. ,	2.81***		
		[3.26]		[0.87]		
Total	1.69***	5.82***	0.35***	0.95***		
	[0.40]	[0.51]	[0.11]	[0.16]		
Reweighting error	-	0.10		0.05		
	[0	0.16]		0.04		
Specification error	-	0.14		0.07		
	[4	0.21]	[	0.08]		

Notes: The between-plant (within-plant) variance is constructed as the variance of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany. Sampling weights are employed. All numbers are given in log percentage points. Bootstraped standard errors (200 replications of the entire procedure) account for clustering at the plant level and are shown in brackets. Asterisks indicate statistical significance at the 1%(\*\*\*), 5%(\*\*), or 10%(\*) level.

 $\textbf{Table 4. Decomposition of Changes in Between-Plant and Within-Plant Quantile Differences}, \\ 1996-2010$ 

T 11.		en-plant	Within-plant		
Inequality measure	50-15	85-50	50-15	85-50	
Total change	18.45***	8.35***	1.36**	1.96***	
	[1.50]	[1.35]	[0.58]	[0.33]	
Composition					
Nationality	-0.06*	0.01	0.02	0.01	
	[0.03]	[0.02]	[0.02]	[0.02]	
Education	0.42**	0.82***	$0.29^*$	0.32***	
	[0.21]	[0.25]	[0.16]	[0.10]	
Age	-0.22**	0.15**	-0.13	0.72***	
	[0.11]	[0.08]	[0.10]	[0.08]	
Occupation	0.03	0.07	0.14	0.47***	
	[0.07]	[0.06]	[0.19]	[0.06]	
Region	-0.22	0.09	0.03	0.00	
0	[0.22]	[0.20]	[0.08]	[0.06]	
Industry	0.99*	1.22*	0.08	-1.29***	
J. Committee of the com	[0.57]	[0.70]	[0.41]	[0.19]	
Plant size	-0.50*	-0.21	0.04	0.27***	
	[0.27]	[0.31]	[0.19]	[0.06]	
Collective bargaining	1.32**	0.04	0.34	$-0.33^*$	
- moon o bar Samming	[0.58]	[0.45]	[0.30]	[0.17]	
Works council	0.26	0.08	0.04	0.05	
WOLKS COULICIT				[0.06]	
Export	[0.25] $-0.01$	[0.20] $0.36$	[0.11] $-0.05$	0.08	
Export					
m 1 1	[0.19]	[0.28]	[0.11]	[0.06]	
Technology	-0.06	0.00	-0.02	0.01	
T	[0.09]	[0.09]	[0.05]	[0.02]	
Investment per worker	0.17	-0.04	0.16	0.09	
	[0.31]	[0.26]	[0.12]	[0.09]	
Total	2.12**	2.58***	0.94*	0.38	
	[0.91]	[1.00]	[0.50]	[0.28]	
Wage structure					
Nationality	0.24	0.00	-0.01	-0.05	
	[0.28]	[0.10]	[0.09]	[0.10]	
Education	5.32***	-0.43	-1.02**	1.19***	
	[1.00]	[0.64]	[0.44]	[0.34]	
Age	-2.24**	-0.55	-0.72	0.02	
	[1.10]	[0.80]	[0.88]	[0.65]	
Occupation	-1.14	-0.45	0.62	0.80***	
	[0.75]	[0.50]	[0.51]	[0.24]	
Region	3.34	4.39*	-1.39	-2.50***	
	[3.23]	[2.50]	[1.10]	[0.61]	
Industry	18.23***	1.62	-1.21	-4.65***	
	[6.86]	[3.74]	[1.48]	[1.06]	
Establishment size	-5.17	[3.74] $1.51$	2.03	-4.67***	
LEGIONESHINGHU SIZC	[4.58]	[4.28]			
Collective bargaining	[4.58] 11.54***		[2.13]	[0.77] $-1.89***$	
Conecuve pargaining	F 3	-1.73	0.44		
Worles occur-:1	[4.42]	[2.49]	[1.29]	[0.67]	
Works council	-9.66**	-2.82	1.03	-1.28**	
D 4	[3.81]	[2.71]	[1.48]	[0.54]	
Export	-1.20	-2.95	-0.38	-0.07	
	[2.39]	[2.15]	[1.03]	[0.49]	
Technology	-5.23*	0.78	0.18	-0.07	
	[2.91]	[1.76]	[0.70]	[0.52]	
Investment per worker	-2.91	-0.81	2.93**	-0.42	
	[4.50]	[2.34]	[1.17]	[0.77]	
Constant	4.50	7.05	-1.68	14.05***	
	[10.39]	[10.09]	[4.63]	[2.20]	
Total	15.64***	5.62***	0.82	0.46	
	[2.00]	[1.39]	[0.83]	[0.41]	
Reweighting error	-0.26	-0.18	0.10	0.20	
iteweighting error		Fr. m. 13	[0.00]	[0.19]	
rteweighting error	[0.34]	[0.34]	[0.22]	[0.13]	
Specification error	$[0.34] \\ 0.95$	[0.34] $0.33$	-0.50	[0.13] 0.92***	

Notes: The between-plant (within-plant) quantile differences are constructed as percentile differences (50-15 and 85-50, respectively) of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany. Sampling weights are employed. All numbers are given in log percentage points. Bootstraped standard errors (200 replications of the entire procedure) account for clustering at the plant level and are shown in brackets. Asterisks indicate statistical significance at the  $1\%({}^{***})$ ,  $5\%({}^{**})$ , or  $10\%({}^*)$  level.

Table 5. Decomposition of Changes in the Overall, Between-Plant, and Within-Plant Variance, 2010–2014

		Within-plant variance		
Total Change -0.47 [0.48]	-0.64 [0.44]	0.18 [0.13]		
Composition Wage structure Composition	Wage structure	Composition	Wage structure	
Nationality $0.08^{***}$ $-0.07$ $0.08^{***}$	-0.09	0.00	$-0.06^*$	
[0.03]   [0.17]   [0.02]	[0.13]	[0.00]	[0.03]	
Education $1.46^{***}$ $-1.49^{***}$ $0.99^{***}$	-1.06***	0.18***	-0.12	
[0.22] $[0.38]$ $[0.20]$	[0.34]	[0.05]	[0.12]	
Age $0.15^{***}$ $-1.00^*$ $0.10^{***}$	-0.12	$0.07^{***}$	-0.23	
[0.04] $[0.56]$ $[0.03]$	[0.46]	[0.02]	[0.16]	
Occupation $0.14^{***}$ $0.31$ $-0.09^{**}$	0.26	0.10***	0.16	
[0.05] $[0.31]$ $[0.04]$	[0.27]	[0.02]	[0.10]	
Region $0.06$ $0.84$ $0.05$	0.66	0.01	0.22	
[0.06] $[0.86]$ $[0.06]$	[0.81]	[0.01]	[0.25]	
Industry $0.23   -0.15   0.27$	-0.89	-0.04	0.81**	
[0.20] $[1.55]$ $[0.22]$	[1.43]	[0.03]	[0.34]	
Plant size $-0.16$ 1.25 $-0.15$	1.32	-0.01	-0.17	
[0.14] $[1.06]$ $[0.14]$	[1.04]	[0.03]	[0.27]	
Collective bargaining $0.05$ $-1.10$ $0.02$	-1.09	0.05***	0.09	
[0.04] $[0.80]$ $[0.04]$	[0.77]	[0.02]	[0.21]	
Works council $0.30^{***}$ 1.10 $0.26^{***}$	$1.20^{*}$	0.02	-0.12	
[0.10] $[0.67]$ $[0.10]$	[0.68]	[0.01]	[0.20]	
Export 0.05 0.72 0.05	0.06	-0.01	0.50***	
[0.04] $[0.60]$ $[0.04]$	[0.57]	[0.01]	[0.18]	
Technology $-0.06$ $1.53^*$ $-0.06$	1.14	0.01	0.08	
[0.05] $[0.79]$ $[0.04]$	[0.79]	[0.01]	[0.23]	
Investment per worker $-0.14^*$ $-1.15$ $-0.09$	-1.39	$-0.05^*$	0.41	
[0.08] $[3.04]$ $[0.10]$	[1.17]	[0.02]	[0.33]	
Constant $-3.03$	-1.70	. ,	-1.70**	
[4.23]	[2.91]		[0.77]	
Total $2.15^{***}$ $-2.23^{***}$ $1.44^{***}$	-1.70***	0.32***	-0.13	
[0.37] $[0.50]$ $[0.35]$	[0.47]	[0.07]	[0.12]	
	0.29***		0.03	
[0.10]	[0.11]	[0	0.02]	
Specification error -0.07	-0.10	0.02		
[0.12]	[0.11]	[0.02]		

Notes: The between-plant (within-plant) variance is constructed as the variance of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in West Germany. Sampling weights are employed. All numbers are given in log percentage points. Bootstraped standard errors (200 replications of the entire procedure) account for clustering at the plant level and are shown in brackets. Asterisks indicate statistical significance at the 1%(\*\*\*), 5%(\*\*), or 10%(\*) level.

Table 6. Decomposition of Changes in the Overall, Between-Plant, and Within-Plant Variance in East Germany, 1996–2010

	Overal	ll variance	Between-p	olant variance	Within-p	lant variance	
Total change	$5.15^{***}$ [0.59]			42*** 0.57]	0.73*** [0.17]		
	Composition	Wage structure	Composition	Wage structure	Composition	Wage structure	
Nationality	0.03	-0.22	0.02	-0.26	0.01	0.00	
	[0.04]	[0.18]	[0.03]	[0.18]	[0.01]	[0.02]	
Education	-0.23	1.72***	-0.09	0.98***	-0.02	0.31**	
	[0.19]	[0.40]	[0.09]	[0.37]	[0.02]	[0.13]	
Age	0.44***	0.21	0.10*	-0.94	0.16***	-0.01	
<u>o</u>	[0.08]	[0.82]	[0.06]	[0.60]	[0.04]	[0.21]	
Occupation	-0.12	0.21	0.01	-0.04	-0.11	[0.29]	
1	[0.13]	[0.38]	[0.03]	[0.29]	[0.11]	[0.18]	
Region	-0.02	1.29	-0.01	1.37	[0.00]	-0.47	
O	[0.05]	[1.60]	[0.04]	[1.49]	[0.01]	[0.33]	
Industry	0.90***	3.74***	0.76**	4.11***	0.18	-0.53	
J J	[0.32]	[1.09]	[0.34]	[1.06]	[0.15]	[0.43]	
Plant size	0.09	1.08	0.12	1.11	-0.08	-0.07	
	[0.15]	[1.23]	[0.23]	[1.28]	[0.11]	[0.45]	
Collective bargaining	$0.45^{**}$	0.64	0.37**	0.78	0.10	-0.17	
	[0.19]	[0.62]	[0.16]	[0.59]	[0.08]	[0.22]	
Works council	0.07	0.60	-0.01	0.46	0.05	0.10	
	[0.08]	[0.66]	[0.04]	[0.61]	[0.04]	[0.23]	
Export	-0.06	-0.75	0.05	-0.67	-0.02	0.03	
	[0.16]	[0.72]	[0.15]	[0.66]	[0.06]	[0.19]	
Technology	0.05	-0.09	-0.01	-0.11	0.04	-0.02	
1001110108)	[0.07]	[0.61]	[0.06]	[0.61]	[0.03]	[0.23]	
Investment per worker	0.24	-1.57	$0.35^{**}$	-1.10	-0.06	-0.14	
investment per werner	[0.13]	[1.19]	[0.15]	[1.15]	[0.06]	[0.32]	
Constant	[0.10]	-2.71	[0.10]	-2.13	[0.00]	1.13	
Constant		[2.85]		[2.76]		[0.89]	
Total	1.84***	4.15***	1.67***	3.55***	0.24	0.44*	
	[0.59]	[0.72]	[0.55]	[0.69]	[0.21]	[0.25]	
Reweighting error	-	0.34	-	0.38	(	0.07	
	[0	0.40]	[1	0.33]	[(	0.17]	
Specification error		0.50		0.42		0.02	
	[0	0.36]	[1	0.32]	[(	0.11]	

Notes: The between-plant (within-plant) variance is constructed as the variance of predicted (residual) wages of a regression of log individual wages on a full set of plant fixed effects. The decomposition is based on LIAB data. The sample includes full-time male workers between 18 and 65 years of age who work in East Germany. Sampling weights are employed. All numbers are given in log percentage points. Bootstraped standard errors (200 replications of the entire procedure) account for clustering at the plant level and are shown in brackets. Asterisks indicate statistical significance at the 1%(\*\*\*), 5%(\*\*), or 10%(\*) level.